Arthur H. Compton (1892 $\sim$ 1962), while at Washington University at St. Louis found that x-rays increase in wave length when scattered, which he explained in 1923 on the basis of the quantum theory of light.

(1) Eo = 
$$m_0 c^2$$
  
For photon,  
 $E = \hbar \omega$  and  $P = \hbar K$   
 $E^2 - c^2 P^2 = 0$   $\omega = c K$ 

For photon, 
$$E = \hbar \omega$$
 and  $P = \hbar K$ 

$$(Photon)_4 = (\hbar \omega, \hbar K, 0, 0)$$

$$\hbar \omega$$

$$(Electron)_4 = (moc^2, 0, 0, 0)$$

$$(Electron)_4 = (mc^2, Pcos(\psi), -Psin(\psi), 0)$$

(2) 
$$KE = \hbar\omega - \hbar\omega' = E - E_0 = mc^2 - m_0c^2$$

(3) 
$$\omega t - Kx = K(ct - x)$$
 (4)  $\omega = cK = 2\pi c/\lambda$ 

(5) 
$$c = f \lambda = (2\pi f) (\lambda / 2\pi) = \omega / K$$

(6) 
$$E^2 - c^2 P^2 = E_0^2$$

$$\lambda' - \lambda = \frac{h}{m_0 C} \{ 1 - \cos(\theta) \}$$